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#### **Key Points:**

- We combine time domain thermoreflectance and diamond cell to measure lattice thermal conductivity of Fe-bearing bridgmanite to 120 GPa
- Thermal conductivity of Fe-bearing bridgmanite drops around 45 GPa due to pressure-induced lattice distortion
- Modeling of LLSVP thermal conductivity and CMB heat flux provides insights to thermo-chemical structure and dynamics of lowermost mantle

Supporting Information:

Supporting Information S1

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# Reduced lattice thermal conductivity of Fe-bearing bridgmanite in Earth's deep mantle

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JGR

Abstract Complex seismic, thermal, and chemical features have been reported in Earth's lowermost mantle. In particular, possible iron enrichments in the large low shear-wave velocity provinces (LLSVPs) could influence thermal transport properties of the constituting minerals in this region, altering the lower mantle dynamics and heat flux across core-mantle boundary (CMB). Thermal conductivity of bridgmanite is expected to partially control the thermal evolution and dynamics of Earth's lower mantle. Importantly, the pressure-induced lattice distortion and iron spin and valence states in bridgmanite could affect its lattice thermal conductivity, but these effects remain largely unknown. Here we precisely measured the lattice thermal conductivity of Fe-bearing bridgmanite to 120 GPa using optical pump-probe spectroscopy. The conductivity of Fe-bearing bridgmanite increases monotonically with pressure but drops significantly around 45 GPa due to pressure-induced lattice distortion on iron sites. Our findings indicate that lattice thermal conductivity at lowermost mantle conditions is twice smaller than previously thought. The decrease in the thermal conductivity of bridgmanite in mid-lower mantle and below would promote mantle flow against a potential viscosity barrier, facilitating slabs crossing over the 1000 km depth. Modeling of our results applied to LLSVPs shows that variations in iron and bridgmanite fractions induce a significant thermal conductivity decrease, which would enhance internal convective flow. Our CMB heat flux modeling indicates that while heat flux variations are dominated by thermal effects, variations in thermal conductivity also play a significant role. The CMB heat flux map we obtained is substantially different from those assumed so far, which may influence our understanding of the geodynamo.

# 1. Introduction

In the past decades, seismic observations combined with mineral physics experiments and geodynamic modeling have revealed an Earth's lowermost mantle more complex than previously expected [cf. Garnero and Mcnamara, 2008]. In particular, the large low shear-wave velocity provinces (LLSVPs) observed by seismic tomography may be associated with strong lateral variations in temperature and composition [Trampert et al., 2004; Mosca et al., 2012; Deschamps et al., 2012]. A likely hypothesis for the compositional anomalies in LLSVPs is that they consist of variations in the iron volume fraction by up to a few percent [Trampert et al., 2004; Deschamps et al., 2012]. Furthermore, the phase transition from bridgmanite to post-perovskite [Murakami et al., 2004] may be locally responsible for abrupt changes in shear- and compressional-wave velocities at the bottom of the lower mantle, referred to as the D" seismic discontinuity [Cobden et al., 2015]. Precise determination of the thermal conductivity, including lattice and radiative components, of the constituting lower mantle materials at relevant conditions would provide critical insight and better constraint on the dynamics of the lowermost mantle and heat flux across core-mantle boundary (CMB) [Lay et al., 2008]. Lateral variations in thermal conductivity triggered by variations in temperature and composition (particularly, iron fraction anomalies) may thus influence the dynamics of LLSVPs, including the generation of thermal plumes at the tops of these provinces, and the amplitude of lateral variations in the CMB heat flux, which have consequences for the geodynamo and the age of the inner core [Buffett, 2000].

Significant efforts have been made to study the lattice and radiative thermal conductivities of the lower mantle materials under extreme conditions, as these two components could play different roles in determining the energy balance and temperature profile in the deep lower mantle. Radiative thermal conductivity of (Fe,AI)-bearing MgSiO<sub>3</sub> bridgmanite at lower mantle conditions has been experimentally measured using optical absorption spectroscopy [*Goncharov et al.*, 2008; *Keppler et al.*, 2008], but the

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**Figure 1.** Schematic drawing of the optical pump-probe measurements for the lattice thermal conductivity of bridgmanite (Bm) samples within a diamond anvil cell. An Al film coated on the Bm substrate is a thermal transducer and absorbs thermal energy from optical pump and probe beams. The pressure is measured by ruby fluorescence. Silicone oil serves as the pressure medium.

reported data remain inconclusive with large uncertainties. In contrast, precise measurements of the lattice thermal conductivity of lower mantle materials under extreme pressure-temperature (P-T) conditions are very challenging [Osako and Ito, 1991; Manthilake et al., 2011]. Thus far, very little experimental data are available and its accuracy is insufficient because of the limitations and difficulties of experimental methods. As a result, current estimates of the lattice thermal conductivity of Earth's lower mantle largely rely on theoretical calculations [Hofmeister, 1999; Haigis et al., 2012; Dekura et al., 2013; Ammann et al., 2014; Tang et al., 2014; Stackhouse et al., 2015] or model extrapolations based on results at relatively low P-T conditions, without consideration of the potential effects of chemical composition at the lowermost mantle conditions. Recently, pulsed lasers coupled with high-pressure diamond anvil cell (DAC) have been applied to

study the lattice thermal conductivity or diffusivity of deep-Earth materials under extreme conditions [*Hsieh et al.*, 2009; *Goncharov et al.*, 2010, 2015; *Ohta et al.*, 2012; *Dalton et al.*, 2013; *Konôpková et al.*, 2016]. Measurements of MgSiO<sub>3</sub> bridgmanite (Mg-Bm) and post-perovskite were reported at pressures up to the CMB but at room temperature [*Ohta et al.*, 2012]. However, to the best of our knowledge, the combined effects of chemical composition and pressure (e.g., the mass disorder of Fe and Al substitution) on the lattice thermal conductivity of Mg-Bm at lowermost mantle pressures have not been experimentally investigated, leading to an incomprehensive understanding of the thermal conductivity and heat transfer of this region. In this paper, we combine time domain thermoreflectance and diamond anvil cell techniques to precisely measure the lattice thermal conductivity of Fe-bearing bridgmanite to 120 GPa. We then apply these results to model radial profiles in thermal conductivity throughout the lower mantle, lateral variations in thermal conductivity of LLSVPs, and heat flux across the CMB.

## 2. Experimental Details

#### 2.1. Starting Materials and Sample Preparation

Chemically homogeneous single crystals of MgSiO<sub>3</sub> bridgmanite and (Fe,Al)-bearing bridgmanites were synthesized at 24 GPa and 1650–1760°C using a Kawai-type multianvil apparatus with a substantially long heating duration for large crystals to grow [*Okuchi et al.*, 2015]. Chemical compositions of the (Fe,Al)-bearing bridgmanites were characterized by an electron probe microanalyzer and determined to be Mg<sub>0.96</sub>Fe<sub>0.07</sub>Si<sub>0.98</sub>O<sub>3</sub> (Fe-Bm) and Mg<sub>0.89</sub>Fe<sub>0.12</sub>Al<sub>0.11</sub>Si<sub>0.89</sub>O<sub>3</sub> (Fe-Al-Bm) [*Okuchi et al.*, 2015], where the Fe and Al contents are representative of those in the lower mantle pyrolite compositional model [*Irifune et al.*, 2010]. Crystalline quality and lattice parameters of the samples from the same capsule were also evaluated using X-ray diffraction at GSECARS of the Advanced Photon Source [*Mao et al.*, 2017]. Each of the bridgmanite crystals was polished down to a thickness of ≈10 µm, coated with ≈80 nm thick Al film and loaded, together with a small ruby ball, into a symmetric DAC with a culet size of 200 or 300 µm. The sample was then pressurized by loading silicone oil (CAS No. 63148-62-9 from ACROS ORGANICS) as the pressure medium, see Figure 1 for the schematic illustration of the sample geometry and experimental setup. The pressure was determined by ruby fluorescence [*Mao et al.*, 1978], and the uncertainties of the pressure measurements were typically <5%.



**Figure 2.** Comparison of example data with calculations by the thermal model for Fe-Bm crystal at high pressures. Example data for the ratio  $-V_{in}/V_{out}$  as a function of delay time between pump and probe pulses are shown as open circles. The solid lines represent calculations by our bidirectional heat flow model with different values of Fe-Bm thermal conductivity  $\Lambda_{Fe-Bm}$ . At (a) 78 GPa and (b) 120 GPa,  $\Lambda_{Fe-Bm} = 11.5$  and 14.5 W m<sup>-1</sup> K<sup>-1</sup>, respectively, provide a best fit using parameters listed in Table 1. In our measurements, the ratio  $-V_{in}/V_{out}$  has strong dependence on the  $\Lambda_{Fe-Bm}$  during delay time of few hundred picoseconds, e.g., 100 to 500 ps [*Cahill and Watanabe*, 2004; *Zheng et al.*, 2007]. A 10% change in  $\Lambda_{Fe-Bm}$  are precise and highly reliable due to the high-quality data and sample geometry.

#### 2.2. High-Pressure Lattice Thermal Conductivity Measurements

After the pressure within the DAC equilibrated and reached a stable value, the lattice thermal conductivity of the bridgmanite was measured at room temperature using time domain thermoreflectance (TDTR). In the TDTR measurement, the output of a mode-locked Ti:sapphire oscillator laser was split into pump and probe beams. The pump beam heated the surface of Al film on the sample, creating temperature variations. The probe beam then detected the resulting changes in the optical reflectivity induced by the temperature changes on the Al film as a function of the time delayed between pump and probe beams. The in-phase  $V_{in}$  and out-of-phase  $V_{out}$  components of the variation of the reflected probe beam intensity, which were synchronous with the 8.7 MHz modulation frequency of the pump beam, were measured using a Si photodiode as well as an RF lock-in amplifier. The details of the TDTR are described elsewhere [*Cahill*, 2004; *Kang et al.*, 2008].

The thermal conductivity of the bridgmanite was determined by comparing the time dependence of the ratio  $-V_{in}/V_{out}$  to calculations based on a thermal model that takes into account heat flow into the sample substrate and into the pressure medium silicone oil [Ge et al., 2006; Schmidt et al., 2008]. Example data with calculations by the thermal model are shown in Figure 2. The thermal model contains several parameters—laser spot size (7.6 μm), thickness of Al film, thermal conductivity, and heat capacity of each layer—but the thermal conductivity of the bridgmanite sample is the only significant unknown and free parameter to be determined. Table 1 lists values of the thermal model parameters we used for the two sets of example data shown in Figure 2. Note that the ratio  $-V_{in}/V_{out}$  at delay time of few hundred picoseconds is sensitive to and scales with the sum of thermal effusivity of bridgmanite and silicone oil divided by the heat capacity per unit area of Al film [Zheng et al., 2007]. The thickness of Al film at ambient pressure was measured in situ by picosecond acoustics, and estimates of the changes in Al thickness at high pressures were described in Chen et al. [2011]: Al thickness decreases by 12% at 25 GPa, by 18% at 60 GPa, and 21% at 120 GPa. Since the thermal penetration depths in the bridgmanite and silicone oil are on the order of hundreds of nanometers at the modulation frequency of the pump beam [Hsieh et al., 2009], the thermal model is insensitive to their thicknesses (~10 µm) (see Figures S1a and S1b in the supporting information). Because the thermal conductivity of Al film at ambient pressure,  $\approx 200 \text{ W m}^{-1} \text{ K}^{-1}$  [Zheng et al., 2007], is large and has no effect on the thermal model calculations (Figure S1c), we fix this value for thermal modeling at high pressures. We estimated the pressure dependence of AI heat capacity from data for the atomic density and elastic constants at high pressures along with calculations of Debye temperature, as described in Hsieh et al. [2009]. The thermal effusivity, square root of the product of thermal conductivity and volumetric heat capacity, of silicone oil at room temperature and up to 24 GPa were taken from *Hsieh* [2015]; for P = 24 to 123 GPa, the thermal effusivity was

Table 1. Input Parameters for the Bidirectional Heat Flow Model at Two Representative Pressures of 78 and 120 GPa											
P (GPa)	$C_{Fe-Bm}$ (J cm <sup>-3</sup> K <sup>-1</sup> )	$C_{AI}$ (J cm <sup>-3</sup> K <sup>-1</sup> )	$h_{AI}\left(nm ight)^{b}$	$e = (\Lambda_{Si}C_{Si})^{1/2}$ (J m <sup>-2</sup> K <sup>-1</sup> s <sup>-1/2</sup> )	<i>r</i> (μm)	h <sub>Fe-Bm/Si oil</sub> (μm)	$(W m^{-1} K^{-1})$	G (MW m <sup>-2</sup> K <sup>-1</sup> )			
78 120	3.39 3.29	2.68 2.72	77.7 76.1	2017 2260	7.6 7.6	10 10	200 200	40 300			

ut Parameters for the Ridiractional Heat Flow Model at Two Penresentative Pressures of 78 and 120 GPa<sup>a</sup>

<sup>a</sup>C<sub>Fe-Bm</sub>: Fe-Bm heat capacity, C<sub>AI</sub>: Al heat capacity, h<sub>AI</sub>: Al thickness, e: silicone oil thermal effusivity, r: laser spot size, h<sub>Fe-Bm</sub>: Fe-Bm thickness, h<sub>Si oil</sub>: silicone oil thickness, Λ<sub>Al</sub>: Al thermal conductivity, *G*: thermal conductance of Al/Fe-Bm and Al/silicone oil interfaces. <sup>b</sup>In this experimental run, the Al thickness at ambient pressure is 96.3 nm.

estimated by extrapolation based on the data below 24 GPa that were fitted into a polynomial, assuming that the silicone oil remains in an amorphous phase at high pressures. Compared to the bridgmanite, the exceptionally low thermal effusivity of silicone oil at high pressures substantially reduces the uncertainty of deriving bridgmanite thermal conductivity as it has only minor effects, typically less than 10% uncertainty, on the thermal model calculations (see Figure S1d). This uncertainty is much smaller than the error propagated when using noble gases (Ar, Ne, He, etc., that solidify at high pressures) or solid pressure media whose thermal conductivities at high pressures are comparable or even larger than the samples.

The heat capacities of the Fe-Bm and Fe-Al-Bm at room temperature and high pressures are unknown. Since the contents of Fe and AI are relatively low, we assume that the pressure dependence of the heat capacities of Fe-Bm and Fe-Al-Bm is close to that of the Mg-Bm taken from Kiefer et al. [2002] and Tsuchiya et al. [2005]; the volumetric heat capacity C = 3.4 J cm<sup>-3</sup> K<sup>-1</sup> at ambient pressure, C = 3.51 J cm<sup>-3</sup> K<sup>-1</sup> at 30 GPa,



Figure 3. Lattice thermal conductivity of bridgmanite at high pressures and room temperature. Data for the Mg-Bm (blue symbols) are in good agreement with literature results [Ohta et al., 2012] (green symbols). The thermal conductivities of Fe-Bm (black symbols) and Fe-Al-Bm (red symbols) are similar to Mg-Bm before  $P \approx 40$  GPa, after which the conductivity of Fe-Bm decreases by ≈20% and then increases slightly with pressure, whereas the conductivity of Fe-Al-Bm increases at a smaller rate with pressure. Each set of symbol shapes represents an individual measurement run, with solid symbols for compression and open symbols for the decompression cycle, respectively. The solid curves show fits to the data for each type of bridgmanite. Literature results for Mg-Bm (orange circle) and mixed with 3 mol % FeSiO<sub>3</sub> (orange diamond) at 26 GPa extrapolated to 300 K from [Manthilake et al., 2011] are plotted for comparison. The light blue shading area indicates the pressure range where the pressure evolution of Fe-Bm and Fe-Al-Bm thermal conductivities changes drastically. The measurement uncertainties are ≈10% before 30 GPa, ≈25% at 60 GPa, and ≈35% at 123 GPa.

 $C = 3.51 \text{ J cm}^{-3} \text{ K}^{-1}$  at 60 GPa, and  $C = 3.3 \text{ J cm}^{-3} \text{ K}^{-1}$  at 123 GPa. We calculated the uncertainty in the thermal conductivity of the bridgmanites caused by uncertainty in each of the parameters used in our thermal model by evaluating the sensitivity of the thermal model to input parameters [see, e.g., Cahill and Watanabe, 2004; Zheng et al., 2007; Hsieh, 2011]; details of the uncertainty evaluation on example tests are shown in Figure S1. We found that uncertainties in all the parameters propagate to ≈10% error in the measured thermal conductivity of the bridgmanites before 30 GPa, ≈25% error at 60 GPa, and ≈35% error at 123 GPa.

## 3. Experimental Results 3.1. Thermal Conductivity of Mg-Bm, Fe-Bm, and Fe-Al-Bm

We precisely measured the lattice thermal conductivities of single-crystal Mg-Bm, Fe-Bm, and Fe-Al-Bm up to pressures near the lowermost mantle, where several seismic complexities are observed, including LLSVPs and the D" discontinuity. The lattice thermal conductivity of single-crystal Mg-Bm (blue symbols in Figure 3) increases monotonically from 5.7 W  $m^{-1}$  K<sup>-1</sup> at ambient pressure to 28.5 W  $m^{-1}$  K<sup>-1</sup> at 117 GPa, in good agreement with literature data for polycrystalline Mg-Bm (green symbols in Figure 3) [Ohta et al., 2012] and theoretical calculations [Dekura et al., 2013; Stackhouse et al., 2015].

As for Fe-bearing Bm, the measured thermal conductivity is similar to the MgSiO<sub>3</sub> end-member before  $P \approx$  40 GPa (black symbols in Figure 3), showing that the effect of Fe substitution on the lattice thermal conductivity of Mq-Bm is small at lower pressures. This behavior is different from the Fe substitution effect on MgO periclase, which results in a significant reduction in thermal conductivity by a factor of  $\approx 10$  at ambient conditions and a much larger pressure dependence when normalized to an ambient value [see Goncharov et al., 2015]. Upon further compression, the thermal conductivity of Fe-Bm abruptly decreases by  $\approx 20\%$  around 40 to 45 GPa, after which the thermal conductivity increases slightly with pressure to  $\approx$ 14.5 W m<sup>-1</sup> K<sup>-1</sup> at 120 GPa, smaller than that of Mg-Bm by a factor of  $\approx$ 2. Recent theoretical and experimental studies showed that the A-site iron ions of Bm lattice undergo an enhanced local lattice distortion with an extremely high hyperfine quadrupole value for Fe<sup>2+</sup> in pressure ranges similar to our study [e.g., Hsu et al., 2010; Mao et al., 2017]. Although the occurrence of the intermediate-spin and low-spin transition of  $Fe^{2+}$  has been proposed, the consensus is that the A-site  $Fe^{2+}$  and  $Fe^{3+}$  remain in the high-spin state, while the B-site  $Fe^{3+}$  undergoes a high-spin to low-spin transition (see section 3.2). We thus attribute the reduced thermal conductivity around 40 to 45 GPa to the pressure-induced lattice distortion of A-site Fe<sup>2+</sup> and Fe<sup>3+</sup> in Fe-Bm, through which the phonon group velocity and phonon densities of states may have changed.

We now turn to the combined effects of Al and Fe substitution on the lattice thermal conductivity of Mg-Bm (red symbols in Figure 3). Again, the lattice thermal conductivity of (Fe,Al)-bearing Bm remains similar to that of Mg-Bm and Fe-Bm until  $P \approx 40$  GPa, after which the conductivity increases in a smaller rate with pressure, and reaches 17.5 W m<sup>-1</sup> K<sup>-1</sup> at 123 GPa. The reduced slope with pressure suggests that the thermal conductivity of Fe-Al-Bm is sensitive to the slight changes in the phonon densities of states and group velocity induced by relatively minimal lattice distortion of *A*-site iron ions (see section 3.2) as well as the enhanced phonon-defect and phonon-boundary scatterings that would suppress the expected increase in the thermal conductivity at higher pressures.

#### 3.2. Pressure-Induced Lattice Distortion in Fe-Bm and Fe-Al-Bm

The ferrous ( $Fe^{2+}$ ) and ferric ( $Fe^{3+}$ ) irons of our Fe-Bm crystal are both largely in the A-site of the perovskite lattice (pseudo-dodecahedral site) based on Mössbauer analysis of our samples, whereas a significant increase in the quadrupole splitting (QS) of  $Fe^{2+}$  occurs between 13 and 32 GPa [Mao et al., 2017]. Such pressure-enhanced QS occurs along with abrupt changes in the bond length and tilting angle of the Fe-O octahedra, as well as in the spontaneous shear strain observed around 40 GPa, and has been attributed to an enhanced lattice distortion (Jahn-Teller effect) of the A-site  $Fe^{2+}$  in the high-spin state [Jackson et al., 2005; Hsu et al., 2010, 2011; Ballaran et al., 2012; Lin et al., 2013; Mao et al., 2017]. Although the occurrence of the extremely high QS component at high pressures was also proposed to be caused by an electronic high-spin to intermediate-spin crossover [Lin et al., 2008; McCammon et al., 2008; Potapkin et al., 2013], recent first-principles calculations [Bengtson et al., 2009; Hsu and Wentzcovitch, 2014; Shukla et al., 2015] show that the intermediate-spin state of  $Fe^{2+}$  is unlikely to occur in the lower mantle conditions. Moreover, equation of state measurements of the Fe-Bm in Mao et al. [2017] did not show an abrupt volume collapse up to 85 GPa, indicating the absence of a pressure-induced high-spin to low-spin crossover in B-site  $Fe^{3+}$  over the investigated pressure range. We therefore conclude that the reduction in our Fe-Bm lattice thermal conductivity observed around 40 to 45 GPa is likely due to the pressure-induced lattice distortion of A-site  $Fe^{2+}$  and  $Fe^{3+}$ , through which the phonon densities of states as well as phonon group velocity may have been slightly altered.

In our Fe-Al-Bm crystals the Fe<sup>2+</sup> and Fe<sup>3+</sup> both occupy the *A*-site and stay in the high-spin state [*Mao et al.*, 2017] over the investigated pressure range. Recently, *Lin et al.* [2016] used X-ray emission, X-ray diffraction, and Mössbauer spectroscopy to study the spin and valence states of iron in the same Fe-Al-Bm sample as ours and did not observe any spin transition up to the pressures of the lowermost mantle. The decrease in the slope of the thermal conductivity with pressure around 40 GPa without a significant reduction as observed in Fe-Bm suggests that the pressure evolution of Fe-Al-Bm thermal conductivity is sensitive to the relatively minimal changes in phonon densities of states and group velocity resulted from the suppressed lattice distortion of *A*-site Fe<sup>2+</sup> and Fe<sup>3+</sup> in Fe-Al-Bm.

### 4. Thermal Conductivity Modeling for Earth's Lower Mantle

The critical influence of Fe substitution on the lattice thermal conductivity of bridgmanite at lowermost mantle revealed by our measurements provides novel insights into the thermo-chemical structure and dynamics of the lower mantle and the CMB heat flux. To quantify the influence of lateral variations in iron on lowermost mantle thermal conductivity, we performed data modeling where we considered the effects of variations in temperature, global iron content ( $dX_{Fe}$ ), and volume fraction of bridgmanite ( $dX_{Bm}$ ), as well as the influence of iron partitioning between bridgmanite and ferropericlase,  $K_D$  [Badro, 2014].

#### 4.1. Effect of Temperature

Temperature dependence of lower mantle minerals' thermal conductivities may be described following

$$\Lambda(T) \propto \frac{K}{T^n},\tag{1}$$

where K is a parameter depending on the material, including its iron content (see below), but not on temperature, and  $0.5 \le n \le 1.0$ . In Mg-Bm, lattice thermal transport is predominantly operated through anharmonic three-phonon scattering; in (Fe,AI)-bearing bridgmanite, however, the three-phonon scattering dominates at low phonon frequency regime and the mass disorder effect plays a critical role at higher frequency regime. As a result, the temperature dependence of the mass disordered Fe-Bm and Fe-Al-Bm would change from a typical  $T^{-1}$  dependence to  $T^{-1/2}$  dependence [Klemens et al., 1962; Dalton et al., 2013]. Such  $T^{-1/2}$  dependence was also reported in other iron-bearing mantle minerals [Xu et al., 2004]. Recent first-principles calculations by Stackhouse et al. [2015] indicate that the temperature dependence of Mg-Bm at deep lower mantle conditions is weaker than the typically assumed  $T^{-1}$  and  $T^{-1/2}$ dependences due to the saturation effect. Stackhouse et al. [2015] showed a consistent Mg-Bm thermal conductivity with other calculations using the typical  $T^{-1}$  dependence [e.g., Dekura et al., 2013; Tang et al., 2014] at moderately high temperature but predicted a larger value at lowermost mantle conditions. For applications to lower mantle thermal conductivity and CMB heat flux (see below), we assumed n = 0.5for Fe-Bm and Fe-Al-Bm. However, to evaluate the influence of n, we further performed a few calculations with n = 1.0. Table S1 in the supporting information shows that for n = 1.0, the thermal contribution to variations in thermal conductivity is enhanced by about a factor of 2, compared to n = 0.5. However, when compositional effects (section 4.2) are also taken into account, thermal conductivity anomalies obtained for n = 0.5 and n = 1.0 are very similar. Furthermore, the impact on CMB heat flux (section 5) is limited, with RMS in relative anomalies in heat flux being only ~10% larger for n = 1.0 than for n = 0.5(Table S1).

Assuming that the temperature dependence of Mg-Bm follows the calculations in *Stackhouse et al.* [2015] and those of Fe-Bm and Fe-Al-Bm follow the  $T^{-1/2}$  dependence, our new data enable lattice thermal conductivity estimation at relevant *P*-*T* conditions near the lowermost mantle ( $\approx$ 120 GPa and 3000 K):  $\approx$ 9 W m<sup>-1</sup> K<sup>-1</sup> for Mg-Bm, 4.6 W m<sup>-1</sup> K<sup>-1</sup> for Fe-Bm, and 5.5 W m<sup>-1</sup> K<sup>-1</sup> for Fe-Al-Bm. Compared to available experimental data for the radiative thermal conductivity of (Fe,Al)-bearing bridgmanite with a similar chemical composition but large uncertainties [*Goncharov et al.*, 2008; *Keppler et al.*, 2008],  $\approx$ 0.5 to 3 W m<sup>-1</sup> K<sup>-1</sup>, our results for the lattice thermal conductivity of (Fe,Al)-bearing bridgmanites at similar *P*-*T* conditions are larger, indicating that the lattice component majorly contributes to the heat transfer in Earth's deep lower mantle. Our findings here challenge previous models [e.g., *Keppler et al.*, 2008; *Goncharov et al.*, 2010] in which the thermal radiation mechanism was expected to be dominant.

Furthermore, deriving equation (1) allows estimating relative variations of thermal conductivity with temperature, which may be written

$$dln\Lambda^{T} = \frac{1}{\Lambda(T_{ref})} \frac{d\Lambda}{dT} dT = -n \frac{dT}{T_{ref}},$$
(2)

where  $dT = (T - T_{ref})$  is the lateral temperature anomaly compared to a reference temperature  $T_{ref}$ . For  $T_{ref}$  in the range of 3000–4000 K, which is typical of CMB temperature [e.g., *Tackley*, 2012], dT = 500 K [*Trampert et al.*, 2004; *Mosca et al.*, 2012], and n = 0.5, thermal conductivity decreases by about 6 to 8%, i.e., smaller than the compositional effect (section 4.2) by at least a factor of 5.



#### 4.2. Effect of Composition

As demonstrated by our measurements, the thermal conductivity of bridgmanite at deep mantle pressures depends on the iron content, which may vary laterally in the deep mantle [*Trampert et al.*, 2004; *Mosca et al.*, 2012]. Assuming that the thermal conductivity of bridgmanite depends linearly on its iron content,  $x_{Fe}^{Bm}$ , it can be calculated using

$$\Lambda_{Bm}(x_{Fe}^{Bm}) = \Lambda_0 + a x_{Fe}^{Bm},$$
 (3)

**Figure 4.** Iron fraction in bridgmanite,  $x_{Fe}^{Bm}$ , and thermal conductivity as a function of iron partitioning,  $K_D$ , and for temperature T = 3000 K, global fraction of iron  $X_{Fe} = 0.09$ , and volume fraction of bridgmanite  $X_{Bm} = 0.8$ .  $\Lambda_{Bm}$  is the thermal conductivity of bridgmanite and is calculated using equation (3) and the corresponding value of  $x_{Fe}^{Bm}$  and iron correction.  $\Lambda_{VRH}$  is the thermal conductivity of mantle aggregate calculated following the Voigt-Reuss-Hill average (equation (7)), with thermal conductivity of ferropericlase assumed to be independent of the iron content and fixed to 24 W m<sup>-1</sup> K<sup>-1</sup> (see text).

where  $\Lambda_0$  is the thermal conductivity for pure Mg-Bm and *a* is a constant that can be inferred from our measurements for Mg-Bm and Fe-bearing bridgmanites. At lowermost mantle pressure (120 GPa and higher) and ambient temperature, our new data indicate that  $\Lambda_0 = 28.5 \text{ W m}^{-1} \text{ K}^{-1}$  and  $\Lambda_{\text{Bm}}(x_{\text{Fe}}^{\text{Bm}} = 0.072) = 14.5 \text{ W m}^{-1} \text{ K}^{-1}$ , leading to  $a = -194.4 \text{ W m}^{-1} \text{ K}^{-1}$ . At lower mantle

temperature, a correction should be performed: for *T* = 3000 K, and assuming that the temperature dependence of Mg-Bm follows the results in *Stackhouse et al.* [2015] and Fe-Bm takes *n* = 0.5 in equation (1),  $\Lambda_0 = 9.0 \text{ W m}^{-1} \text{ K}^{-1}$  and  $\Lambda_{\text{Bm}}(x_{\text{Fe}}^{\text{Bm}} = 0.072) = 4.6 \text{ W m}^{-1} \text{ K}^{-1}$ , which leads to *a* = -61.1 W m<sup>-1</sup> K<sup>-1</sup>. From equation (3), one can define relative anomalies in thermal conductivity due to iron anomalies, with respect to a reference conductivity  $\Lambda_{\text{Bm,ref}}$  taken at reference value  $x_{\text{Fe,ref}}^{\text{Bm}}$ ,

$$d\ln\Lambda_{\rm Bm}^{\rm Fe} = \frac{1}{\Lambda_{\rm Bm,ref}} \frac{\partial\Lambda_{\rm Bm}}{\partial x_{\rm Fe}^{\rm Bm}} dx_{\rm Fe}^{\rm Bm} = \frac{a}{\Lambda_{\rm Bm,ref}} \left(\frac{T_0}{T_{\rm ref}}\right)^n dx_{\rm Fe}^{\rm Bm}$$
(4)

where  $dx_{Fe}^{Bm} = (x_{Fe}^{Bm} - x_{Fe,ref}^{Bm})$  is the excess iron in bridgmanite;  $T_0 = 300$  K is the ambient temperature, at which our thermal conductivity measurements were conducted; and a = -194.4 W m<sup>-1</sup> K<sup>-1</sup> the iron correction. The assumption that the thermal conductivity of bridgmanite varies linearly with  $x_{Fe}^{Bm}$  may become invalid if  $x_{Fe}^{Bm}$  is too large compared to that of our samples ( $x_{Fe}^{Bm} = 0.072$ ). In particular, due to saturation effect, the thermal conductivity of bridgmanite may no longer be reduced for values of  $x_{Fe}^{Bm}$  larger than a threshold value. Importantly, in the lower mantle the fraction of iron in bridgmanite likely varies by only a few percent, remaining in the range of 0.05–0.10 (see next paragraphs and Figures 4 and S2), i.e., close to the iron content of our samples. It is therefore reasonable to assume that in the case of the lower mantle, the thermal conductivity of bridgmanite would require additional experiments, e.g., for  $x_{Fe}^{Bm}$  around 0.05 and 0.1. In addition, the  $T^{-1/2}$  dependence has been reported to reasonably well describe the temperature dependence of thermal conductivity of crystals mixed with impurities [see, e.g., *Klemens et al.*, 1962; *Xu et al.*, 2004; *Dalton et al.*, 2013], among which the crystals and contents of impurities are different from each other. This suggests that in our case, it is reasonable to assume that the effect of temperature is independent of the iron content, in particular when the variation of iron content in bridgmanite is small.

Variations of iron in the Earth's mantle are usually parameterized in terms of the global volume fraction of iron oxide (FeO),  $X_{\text{Fe}}$ , given by

$$X_{\rm Fe} = X_{\rm Bm} x_{\rm Fe}^{\rm Bm} + (1 - X_{\rm Bm}) x_{\rm Fe}^{\rm Fp},$$
 (5)

where  $X_{Bm}$  is the volume fraction of bridgmanite in the aggregate and  $x_{Fe}^{Bm}$  and  $x_{Fe}^{Fp}$  are the individual iron fractions in bridgmanite and ferropericlase. For given values of  $X_{Fe}$  and  $X_{Bm}$ , the iron fraction in

bridgmanite,  $x_{Fe}^{Bm}$ , can be obtained by prescribing the iron partitioning between bridgmanite (Mg,Fe)SiO<sub>3</sub> and ferropericlase (Mg,Fe)O,

$$K_{D} = \frac{x_{Fe}^{Bm} / (1 - x_{Fe}^{Bm})}{x_{Fe}^{Fp} / (1 - x_{Fe}^{Fp})},$$
(6)

and by solving equations (5) and (6) (see Appendix A1). In the Earth's lower mantle, iron goes preferentially to ferropericlase, i.e.,  $K_D < 1$ . High-pressure mineral physics experiments and ab initio calculations further indicate that its value is in the range of 0.1–0.5 [e.g., *Badro*, 2014]. As an example, the brown curve in Figure 4 plots the iron fraction in bridgmanite,  $x_{Fe}^{Bm}$ , as a function of the iron partitioning, and for  $X_{Bm} = 0.8$  and  $X_{Fe} = 0.09$ , which are typical of Earth's average mantle. For these values,  $x_{Fe}^{Bm}$  is equal to 0.056 and 0.072 for  $K_D = 0.2$  and  $K_D = 0.4$ , respectively. Figure S2 plots variations of the iron fraction in bridgmanite,  $dX_{Fen}^{Bm}$ , as a function of variations in the global fraction of iron,  $dX_{Fe}$ , and in the volume fraction of bridgmanite,  $dX_{Bm}^{Bm}$ . The reference iron fraction,  $x_{Fe,ref}^{Bm}$ , is taken at  $X_{Fe,ref} = 0.09$  and  $X_{Bm,ref} = 0.8$  (brown curve in Figure 4). An increase in the global iron fraction of 0.03 ( $X_{Fe} = 0.12$ ) combined with an increase in the fraction of bridgmanite of 0.1 ( $X_{Bm} = 0.9$ ), typical of the variations found in LLSVPs [*Trampert et al.*, 2004; *Mosca et al.*, 2012], leads to an excess of the iron fraction in bridgmanite of 0.039 ( $x_{Fe}^{Bm} = 0.095$ ) for  $K_D = 0.2$ , and 0.036 ( $x_{Fe}^{Bm} = 0.108$ ) for  $K_D = 0.4$ .

The thermal conductivity of the lower mantle may be estimated by averaging thermal conductivities of individual minerals constituting the mantle aggregate, according to the relative proportion of these minerals. Here we define mantle thermal conductivity with a Voigt-Reuss-Hill (VRH) average. VRH average is commonly used to calculate the thermo-elastic properties of mantle minerals and is defined as the average of arithmetic and harmonic means. For an aggregate composed of two minerals (in our case, bridgmanite and ferropericlase), the VRH average of thermal conductivity writes as

$$\Lambda_{\rm VRH} = \frac{1}{2} \left[ X_{\rm Bm} \Lambda_{\rm Bm} + (1 - X_{\rm Bm}) \Lambda_{\rm Fp} + \frac{\Lambda_{\rm Bm} \Lambda_{\rm Fp}}{(1 - X_{\rm Bm}) \Lambda_{\rm Bm} + X_{\rm Bm} \Lambda_{\rm Fp}} \right],\tag{7}$$

where  $\Lambda_{Bm}$  and  $\Lambda_{Fp}$  are the thermal conductivities of bridgmanite and ferropericlase, respectively. Note that for the electrical conductivity of a representative mantle aggregate, VRH average has been shown to be biased toward the upper Hashin-Shtrikman bound [e.g., Khan and Shankland, 2012; Deschamps and Khan, 2016], which is considered as the upper possible bound for a multiphase aggregate. Because the thermal conductivities of bridgmanite and ferropericlase differ by less than 1 order of magnitude (see discussion below), such bias might be limited and smaller than experimental uncertainties. Interestingly, preliminary calculations indicate that for thermal conductivity, VRH average is close to the geometric average of Hashin-Shtrikman bounds. The thermal conductivity of bridgmanite as a function of x<sub>Fe</sub><sup>Bm</sup> is calculated using equation (3), with  $x_{Fe}^{Bm}$  being given by equation (A2). For the conductivity of ferropericlase, we used the data of Goncharov et al. [2015] for Mg<sub>0.9</sub>Fe<sub>0.1</sub>O extrapolated at 120 GPa and assumed that it does not depend on the iron content, leading to  $\Lambda_{Fp}$  = 76 W m<sup>-1</sup> K<sup>-1</sup> at room temperature. We further assumed that the temperature dependence of ferropericlase conductivity is similar to that of Fe-bearing bridgmanite, with n = 0.5 in equation (1), leading to  $\Lambda_{\rm Fp} = 24$  W m<sup>-1</sup> K<sup>-1</sup> at T = 3000 K. Note that variations in the volume fraction of bridgmanite,  $X_{Bm}$ , induce changes in the aggregate thermal conductivity,  $\Lambda_{VRH}$ , directly through equation (7), and indirectly by partially controlling the fractions of iron in bridgmanite and ferropericlase. Relative variations in the mantle conductivity due to variations in the volume fraction of bridgmanite and in the global volume fraction of iron are obtained by deriving equation (7) with respect to  $X_{Bm}$  and  $X_{Fe}$  following

$$dIn\Lambda_{VRH}^{Bm} = \frac{1}{\Lambda_{VRH}} \frac{\partial \Lambda_{VRH}}{\partial X_{Bm}} dX_{Bm} = \frac{(\Lambda_{Bm} - \Lambda_{Fp})}{2\Lambda_{VRH}} \left\{ 1 + \frac{\Lambda_{Bm}\Lambda_{Fp}}{\left[(1 - X_{Bm})\Lambda_{Bm} + X_{Bm}\Lambda_{Fp}\right]^{2}} \right\} dX_{Bm} + \frac{1}{\Lambda_{VRH}} \left( \frac{\partial \Lambda_{VRH} \partial \Lambda_{Bm}}{\partial \Lambda_{Bm} \partial X_{Bm}} + \frac{\partial \Lambda_{VRH} \partial \Lambda_{Fp}}{\partial \Lambda_{Fp} \partial X_{Bm}} \right) dX_{Bm}$$
(8)

and

$$dln\Lambda_{\rm VRH}^{\rm Fe} = \frac{1}{\Lambda_{\rm VRH}} \frac{\partial\Lambda_{\rm VRH}}{\partial X_{\rm Fe}} dX_{\rm Fe} = \frac{1}{\Lambda_{\rm VRH}} \left( \frac{\partial\Lambda_{\rm VRH}}{\partial\Lambda_{\rm Bm}} \frac{\partial\Lambda_{\rm Bm}}{\partial X_{\rm Fe}} + \frac{\partial\Lambda_{\rm VRH}}{\partial\Lambda_{\rm Fp}} \frac{\partial\Lambda_{\rm Fp}}{\partial X_{\rm Fe}} \right) dX_{\rm Fe}, \tag{9}$$



**Figure 5.** Profiles of the lattice thermal conductivity of bridgmanite along a model lower mantle geotherm (see section 4.3) with dotted curves showing uncertainties. These profiles are derived by extrapolating the room temperature data fits in Figure 3 to high temperature with respective temperature dependences described in the text.

where partial derivatives involved in equations (8) and (9) are given in Appendix A2 (equations (A4) to (A9)). According to equation (3),  $\partial A_{Bm} / \partial x_{Fe}^{Bm} = a(T_0/T_{ref})^n$ , where  $T_0 = 300$  K is the ambient temperature at which our thermal conductivity measurements were performed, and a = -194.4 W m<sup>-1</sup> K<sup>-1</sup>. Furthermore, since we assumed that the conductivity of ferropericlase does not depend on the iron content,  $\partial \Lambda_{VRH} / \partial x_{Fe}^{Fp} = \partial \Lambda_{Fp} / \partial x_{Fe}^{Fp} = 0$ .

# 4.3. Radial Profile of Lower Mantle Thermal Conductivity

Figure 5 shows profiles of the lattice thermal conductivity of bridgmanite along a model lower mantle geotherm, which we here define with a linear interpolation between *P-T* conditions at depths of 700 km (25 GPa, 2050 K) and 2620 km (120 GPa, 3000 K):

 $T_{\text{geotherm}}(K) = 2050 + (P-25) \times 10$ , where P is in GPa. Note that variations of the extrapolated lattice thermal conductivity profiles in the lower mantle using other representative geotherms are relatively small and within the uncertainty of our modeled profiles shown in Figure 5. Along this geotherm, the thermal conductivity of Fe-Bm drops from  $\approx$ 5.6 to 4.5 W m<sup>-1</sup> K<sup>-1</sup> around 45 GPa ( $\approx$ 1100 km depth), while the thermal conductivity of Mg-Bm continuously increases with increasing depth. The thermal conductivity of Fe-Bm is approximately half of the Mg-Bm at the lowermost mantle. Because bridgmanite is the most abundant mineral in the lower mantle, the sudden drop around 45 GPa and subsequent reduction of the thermal conductivity compared to Mg-Bm throughout the lower mantle are likely to induce a comparable reduction in the mantle thermal conductivity. Interestingly, tomographic images have shown that some (but not all) slabs are stacked around 1000 km [e.g., Fukao and Obayashi, 2013], which was recently attributed to an increase in viscosity in the depth range of 800–1200 km inferred from analysis of the long wavelengths of the geoid [Rudolph et al., 2015]. A sudden decrease in the thermal conductivity of Fe-Bm at mid-lower mantle depths, as suggested by our results, would, on the contrary, promote mantle flow, facilitating slabs crossing over the 1000 km barrier and sinking into the deeper mantle. Because the deviation of Fe-Bm thermal conductivity from the Mg-Bm substantially increases with depth, the descent of the subducted slabs in the lowermost mantle would be further accelerated. The decrease in the thermal conductivity, together with other effects that remain to be identified, may thus compensate the previously expected viscosity barrier at approximately 1000 km, and eventually allow slabs to reach the bottom of the mantle, as indicated by tomographic images. This scenario modifies our current view of the deep mantle dynamics and could be tested by numerical models of convection including, among other complexities, a depth-dependent thermal conductivity.

#### 4.4. Lateral Variations in the Thermal Conductivity at the Lowermost Mantle

Figure 6a plots the relative variations in thermal conductivity of bridgmanite due to variations in iron,  $d\ln \Lambda_{Bm}^{Fe}$  (equation (4)), as a function of the anomalies in the global iron content and volume fraction of bridgmanite,  $dX_{Fe}$  and  $dX_{Bm}$ , and for iron partitioning  $K_D = 0.25$  (for other values of  $K_D$ , see Figure S3). For each iron partitioning, the reference value,  $\Lambda_{Bm,ref}$ , is calculated at  $X_{Fe,ref} = 0.09$  and  $X_{Bm,ref} = 0.8$  (dark blue curve in Figure 4). For  $dX_{Fe} = 0.03$  and  $dX_{Bm} = 0.1$ , typical of the compositional anomalies that may be found in LLSVPs [*Trampert et al.*, 2004], and for  $K_D = 0.25$ , the lattice thermal conductivity of Fe-bearing bridgmanite decreases by 45% compared to its reference value at  $X_{Fe} = 0.09$  and  $X_{Bm} = 0.8$ .

We then calculated variations in the thermal conductivity of an aggregate (VRH average) of bridgmanite and ferropericlase at temperature  $T_{ref}$  = 3000 K and lowermost mantle pressure, where the conductivity of



**Figure 6.** Relative variations in thermal conductivity (color scale) due to variations in global iron content,  $X_{Fe'}$  and volume fraction of bridgmanite,  $X_{Bm}$ . (a) Variations in bridgmanite conductivity,  $\Lambda_{Bm}$ , due to variations in iron fraction in bridgmanite,  $X_{Fe'}^{Bm}$  (equation (4)). (b) Variations in conductivity of a bridgmanite-ferropericlase aggregate (VRH average),  $\Lambda_{VRH}$ , due to variations in  $X_{Bm}$  (equation (8)). (c) Variations in  $\Lambda_{VRH}$  due to variations in  $X_{Fe}$  (equation (9)). (d) Variations in  $\Lambda_{VRH}$  due to combined variations in  $X_{Fe}$  and  $X_{Bm}$ . Reference values are  $X_{Fe,ref} = 0.09$  and  $X_{Bm,ref} = 0.8$ , respectively, and iron partitioning,  $K_{D}$ , is equal to 0.25 (see Figures S3 and S4 for other values). Calculations are made at the lowermost mantle pressure, P = 120 GPa, and reference conductivities are shown in Figure 4.

ferropericlase,  $\Lambda_{\rm Fp} = 24 \text{ W m}^{-1} \text{ K}^{-1}$ , was extrapolated from recent experiments [*Goncharov et al.*, 2015]. Figures 6b–6d plot dln $\Lambda_{\rm VRH}^{\rm Bm}$  (equation (8)), dln $\Lambda_{\rm VRH}^{\rm Fe}$  (equation (9)), and their combined effect for iron partitioning  $K_D = 0.25$  (for other values of  $K_D$ , see Figure S4). The total influence of  $X_{\rm Bm}$ , including its effect on  $x_{\rm Bm}^{\rm Fe}$ , is larger than that of  $X_{\rm Fe}$  alone and gets larger with decreasing iron partitioning. For  $K_D = 0.25$ ,  $dX_{\rm Fe} = 0.03$ , and  $dX_{\rm Bm} = 0.1$ , the decrease in the aggregate thermal conductivity due to changes in iron and brigdmanite content reaches 21% and 30%, respectively. Importantly, the combined effect of  $X_{\rm Bm}$  and  $X_{\rm Fe}$  remains strong, with a reduction of conductivity due to a temperature anomaly of 500 K ranges between 6% and 8% depending on the reference temperature.

Finally, we calculated thermal conductivity anomalies associated with the thermo-chemical model from probabilistic tomography [*Trampert et al.*, 2004]. This thermo-chemical model of Earth's mantle includes lateral variations in temperature, global iron (FeO) content, and volume fraction of brigmanite (Figures 7a–7c). Updated models [*Mosca et al.*, 2012] include a finer radial parameterization and variations in post-perovskite at the bottom of the mantle. However, since we did not perform thermal conductivity measurements for this mineral, we preferred using *Trampert et al.* [2004] model. Note that thermo-chemical models derived from probabilistic tomography are limited to spherical harmonic degrees 2, 4, and 6. Following a scaling procedure based on the partitioning of odd and even degrees in classical tomography,



**Figure 7.** Distributions of anomalies in (a) temperature, (b) global iron content, and (c) volume fraction of bridgmanite derived from probabilistic tomography *Trampert et al.* [2004]. (d) CMB heat flux calculated from temperature anomalies in Figure 7a, and neglecting variations of thermal conductivity with temperature and composition,  $dln\Phi = -dT/\Delta T_{ref}$ , assuming  $\Delta T_{ref} = 750$  K.

Amit et al. [2015] attempted recovering odd degrees of temperature distribution of Mosca et al. [2012] to build CMB heat flux. Interestingly, the resulting temperature pattern does not substantially differ from that containing even degrees only. Our calculations (Figures 8a–8c and Table 2) show that in LLSVPs, an excess in iron and bridgmanite leads to conductivity anomalies with a root-mean-square (RMS) amplitude of  $\approx$ 15% and a maximum decrease (increase) of up to 38% (24%). The thermal effect (Figure 8c) is smaller, with RMS amplitude anomalies of  $\approx$ 3%. Such variations in lower mantle thermal conductivity may have important consequences for lower mantle dynamics. A decrease in the thermal conductivity of the constituting lower mantle materials, including bridgmanite, is expected to promote thermal convection in the region. Low thermal conductivity mapped in LLSVPs (Figures 8a–8c) would enhance internal flow within these regions and the generation of thermal plumes at the tops of these provinces. By contrast, if LLSVPs are not animated by convection, a lower thermal conductivity would reduce heat transfer and favor the heating up of LLSVPs.

An effect that is not accounted for in our thermal conductivity maps is the presence of post-perovskite. Experiments [*Ohta et al.*, 2012] reported that post-perovskite conductivity is larger than that of bridgmanite by about 60%. The amount and distribution of post-perovskite depend on the CMB temperature and on lateral variations in temperature. Based on our current understanding of the mineral physics and seismic properties, post-perovskite may be more likely present in D" zones as patches extending up to about 200–300 km above the CMB, and outside the LLSVPs, usually considered to be hotter than surrounding regions. The possible presence of post-perovskite in D" zones would then enhance the thermal conductivity contrast induced by variations in iron content predicted by our models (Figures 8a–8c).

In addition, our modeling of lower mantle thermal conductivity does not take into account the effect of radiative thermal conductivity. Given the limited available data with large uncertainty ( $\approx$ 0.5 to 3 W m<sup>-1</sup> K<sup>-1</sup>) [Goncharov et al., 2008; Keppler et al., 2008], the radiative thermal conductivity of (Fe,AI)-bearing bridgmanite at expected lowermost mantle *P-T* conditions is approximately 10–60% of our results for the lattice thermal conductivity ( $\approx$ 4.6 and 5.5 W m<sup>-1</sup> K<sup>-1</sup>; see Figure 5). As a result, the *total* thermal conductivity may be

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**Figure 8.** Relative variations in (a–c) thermal conductivity and (d–f) core-mantle boundary heat flux in the lowermost mantle (2000–2891 km). Thermal conductivity is obtained from the Voigt-Reuss-Hill (VRH) average of bridgmanite and ferropericlase. Figures 8a–8c show relative variations in conductivity due to global iron content (dln $\Lambda^{Fe}$ , equation (9)), volume fraction of bridgmanite (dln $\Lambda^{Bm}$ , equation (8)), and temperature (dln $\Lambda^{T}$ , equation (2) with n = 0.5), respectively. Figures 8d and 8e map the relative heat flux anomalies due to variations in thermal conductivity with composition (third and fourth terms in the right-hand-side of equation (14)), and the relative heat flux anomalies due to variations in temperature and to their effects on conductivity (first and second terms in the right-hand-side of equation (14)). Figure 8f shows the total relative heat flux anomalies (equation (14)). Thermo-chemical distributions are from *Trampert et al.* [2004], iron partitioning is assumed to be constant,  $K_D = 0.25$ , reference thermochemical state is  $X_{Bm,ref} = 0.8$ ,  $X_{Fe,ref} = 0.09$ , and  $T_{ref} = 3000$  K, and CMB temperature  $T_{CMB} = 3750$  K. Calculations are made at the lowermost mantle pressure, P = 120 GPa.

increased by approximately 10–60%, comparable to the uncertainty of our data ( $\approx$ 35%) at lowermost mantle *P-T* conditions, when we take into account the radiative component. However, the effects of composition and temperature on the radiative thermal conductivity of (Fe,Al)-bearing bridgmanite have not been well characterized quantitatively. Sensitivity of radiative conductivity to temperature has an opposite trend to that of the lattice conductivity and may partially balance it, which would overall reduce the variations of thermal conductivity with temperature. The changes in both thermal conductivities induced by temperature anomaly at very high temperature condition of the lowermost mantle are expected to be relatively small, as suggested by Figure 8c. The compositional effect on the radiative conductivity is not well constrained, but assuming that its trend is similar to that on the lattice conductivity, we expect that the inclusion of radiative conductivity would only have minor influences on our modeling results. In particular, the decrease in the thermal conductivity of LLSVPs due to iron fraction anomaly would still be present, and the relative lateral variations of CMB heat flux pattern would be unchanged (see section 5).

Quantity	RMS	Minimum	Maximum	$q^*$
Thermo-chemical Anomalies				
1T	182.61	-475.60	336.20	-
dX <sub>Bm</sub>	0.0431	-0.0835	0.0926	-
dX <sub>Fe</sub>	0.0098	-0.0182	0.0264	-
Thermal Conductivity Anomalies				
$d\ln \Lambda_{-}^{Bm}$	0.1058	-0.2528	0.1877	-
dln∆_ <sup>Fe</sup>	0.0558	-0.1744	0.0994	-
dln∆ <sup>l</sup>	0.0304	-0.0560	0.0793	-
dln∆	0.1455	-0.3784	0.2469	-
Heat Flux Anomalies				
dln $\Phi$ ( $\Lambda$ constant)	0.2435	-0.4483	0.6341	0.54
$d\ln\Phi_{-}^{C} = d\ln\Lambda^{Bm} + d\ln\Lambda^{Fe}$	0.1460	-0.3695	0.2210	0.30
$d\ln\Phi^{T} = - dT/\Delta T_{ref} + d\ln\Lambda^{T}$	0.2739	-0.5043	0.7134	0.61
dlnΦ	0.2943	-0.4921	0.7651	0.63

**Table 2.** Root-Mean-Square (RMS), Minimum and Maximum in Thermo-chemical Distributions, Thermal Conductivity, and Heat Flux Relative Anomalies, and  $q^*$  Parameter<sup>a</sup>

<sup>a</sup>Thermo-chemical anomalies are from *Trampert et al.* [2004]. Thermal conductivity anomalies due to changes in temperature (dln $\Lambda^T$ ), volume fraction of bridgmanite (dln $\Lambda^{Bm}$ ), and iron content (dln $\Lambda^{Fe}$ ) are given by equations (2), (8), and (9), respectively. For dln $\Lambda^T$ , temperature exponent in equation (2) is set to n = 0.5. Heat flux variations due to anomalies in temperature (dln $\Phi^T$ ) are given by the sum of the first and second terms in the right-hand side of equation (14),  $- dT(\varphi, \theta)/\Delta T_{ref} + dln \Lambda^T$ , and heat flux variations due to anomalies in composition (dln $\Phi^C$ ) are given by the sum of the third and fourth terms, dln $\Lambda^{Bm} + dln \Lambda^{Fe}$ . The CMB temperature is fixed to  $T_{CMB} = 3750$  K, the reference temperature and composition are  $T_{ref} = 3000$  K (leading to  $\Delta T_{ref} = 750$  K),  $X_{Bm,ref} = 0.8$ ,  $X_{Fe,ref} = 0.09$ , and the iron partitioning is set to  $K_D = 0.25$ . Calculations are made at lowermost mantle pressure, P = 120 GPa.

### 5. Implications for Heat Flux at the Core-Mantle Boundary

Variations in lowermost mantle thermal conductivities triggered by thermal and compositional changes may influence lateral variations in CMB heat flux and have implications for geodynamo. CMB heat flux is a key parameter controlling the extraction of heat from the core. Its amplitude and lateral variations may be used as a boundary condition for models of the geodynamo, thus influencing the outer core flow and the generated geomagnetic field. At a given longitude  $\varphi$  and latitude  $\theta$ , the CMB heat flux is given by

$$\Phi(\varphi,\theta) = \Lambda(\varphi,\theta) \frac{[T_{\mathsf{CMB}} - T(\varphi,\theta,D)]}{D},$$
(10)

where the temperature at the CMB,  $T_{CMB}$ , is assumed constant, and T and  $\Lambda$  are the temperature and thermal conductivity at location  $\varphi$ ,  $\theta$ , and altitude D above the CMB. Physically, the value of D should be equal to the thickness of the thermal boundary layer at the bottom of the mantle, i.e., the region where the depth-increase of temperature is superadiabatic. This value is not well constrained but may reach a few hundreds of kilometers. Practically, because we are only mapping relative variations in heat flux, our heat flux maps do not depend on the value of D (equation (14)). It is, however, important to choose the temperature distribution not too close to CMB. The thermo-chemical model we use [*Trampert et al.*, 2004] samples the depth range of 2000–2891 km, and thus satisfies this requirement.

Both lateral variations in temperature and in thermal conductivity control lateral variations in CMB heat flux: increasing temperature decreases the vertical temperature gradient, and therefore reduces the heat flux; and heat flux decreases with thermal conductivity, which varies locally with temperature and with composition (see previous sections). Lateral variations in heat flux relative to a reference heat flux  $\Phi_{ref}$  may be decomposed in variations due to anomalies in the radial temperature jump,  $\Delta T$ , and anomalies in thermal conductivity,  $\Lambda$ , following

$$\mathsf{dln}\ \Phi(\varphi,\theta) = \frac{1}{\varPhi_{\mathsf{ref}}} \left[ \left( \frac{\partial \Phi}{\partial \Delta T} \right)_{\Lambda = \Lambda_{\mathsf{ref}}} d\Delta T + \left( \frac{\partial \Phi}{\partial \Lambda} \right)_{\Delta T = \Delta T_{\mathsf{ref}}} d\Lambda \right] = \frac{(\Delta T - \Delta T_{\mathsf{ref}})}{\Delta \mathsf{T}_{\mathsf{ref}}} + \mathsf{dln}\ \Lambda, \tag{11}$$

where  $\Phi_{ref}$  is taken at reference temperature  $T_{ref}$  and reference thermal conductivity  $\Lambda_{ref}$ .

$$\Phi_{\rm ref} = \Lambda_{\rm ref} \frac{[T_{\rm CMB} - T_{\rm ref}]}{D}.$$
(12)



**Figure 9.** (a) Root-mean-square (RMS) in dln $\Phi$  (equation (14)) neglecting (green curve) and taking into account (red curve) lateral variations in thermal conductivity with temperature and composition. The blue curve plots the relative ratio between the RMS of thermal and compositional contributions to dln $\Phi$ . Results are plotted as a function of the reference vertical temperature jump,  $\Delta T_{ref}$ . (b) The  $q^*$  parameter (equation (15)) as a function of  $\Delta T_{ref}$  for purely thermal and compositional contributions (blue curve) and for thermal and compositional contributions (blue curve). For comparison, the green curve shows the  $q^*$  parameter obtained when neglecting the lateral variations in conductivity.

Noting that the radial temperature jump at a given location,  $\Delta T$ , can be decomposed as

$$\Delta T(\varphi, \theta) = \Delta T_{\mathsf{ref}} - \mathsf{d} T(\varphi, \theta), \quad (13)$$

where  $\Delta T_{ref} = (T_{CMB} - T_{ref})$  is the radial temperature jump at  $T_{ref}$  and  $dT(\varphi,\theta)$  the lateral variation in temperature, and splitting dln $\Lambda$  in its thermal (equation (2)) and compositional (equations (8) and (9)) contributions, the lateral relative variations in heat flux can be written as the sum of lateral variations in temperature relative to the mean radial temperature jump, and lateral relative variations in thermal conductivity due to lateral changes in temperature and composition, i.e.,

$$\begin{split} \mathrm{dln} \ \Phi(\varphi,\theta) &= -\frac{dT(\varphi,\theta)}{\Delta T_{\mathsf{ref}}} \\ &+ \mathrm{dln}\Lambda^T + \mathrm{dln}\Lambda^{\mathsf{Bm}} \\ &+ \mathrm{dln}\Lambda^{\mathsf{Fe}}, \end{split} \tag{14}$$

where d*T* is the temperature anomaly with respect to reference temperature  $T_{ref}$ ,  $\Delta T_{ref} = (T_{CMB} - T_{ref})$  is the mean radial temperature jump,  $T_{CMB}$  is the CMB temperature, and dln $\Delta^{T}$ , dln $\Delta^{Bm}$ , and dln $\Delta^{Fe}$  are the relative conductivity anomalies due to variations in temperature, fraction of bridgmanite, and iron content, respectively. Note that the first term in the right-hand-side of equation (14),  $-dT/\Delta T_{ref}$ , represents the heat

flux variations due to temperature variations alone, i.e., neglecting the variations in thermal conductivity. This contribution is mapped in Figure 7d, assuming  $\Delta T_{ref} = 750$  K. Equation (14) requires the knowledge of the CMB temperature ( $T_{CMB}$ ) and of the reference mantle geotherm ( $T_{ref}$ ), which are both not well constrained. These values, or equivalently the value of  $\Delta T_{ref}$ , are controlling the relative influence of heat flux variations due to temperature anomalies and its effect on thermal conductivity (given by the sum of the first and second terms in the right-hand-side of equation (14),  $dln\Phi^T = - dT/\Delta T_{ref} + dln\Lambda^T$ ) and compositional anomalies (given by  $dln\Phi^C = dln\Lambda^{Bm} + dln\Lambda^{Fe}$ ) (Figure 9a).

The results of our modeling for the Earth's lowermost mantle show that heat flux anomalies at the CMB are dominated by thermal effects (Figures 8d–8f and Table 2). For these calculations, we used, again, the bottom layer (2000–2891 km) of the 3-D thermo-chemical model from probabilistic tomography [*Trampert et al.*, 2004], iron partitioning  $K_D = 0.25$ , a reference thermo-chemical state defined by  $X_{Bm,ref} = 0.8$ ,  $X_{Fe,ref} = 0.09$ ,  $T_{ref} = 3000$  K, and a CMB temperature  $T_{CMB} = 3750$  K (leading to  $\Delta T_{ref} = 750$  K). Table 2 lists root-mean-square (RMS) and minimum and maximum values of lateral relative variations in thermal conductivity and heat flux. Note that because the distributions in temperature and composition in *Trampert et al.* [2004] are not perfectly correlated, the relative anomalies dln $\Lambda^{Bm}$ , dln $\Lambda^{Fe}$ , and dln $\Lambda^{T}$  are also not correlated, and therefore, the sum of their RMS is different from the RMS of their sum. Figures 8d–8f and Table 2 indicate that heat flux variations are dominated by the thermal contribution, dln $\Phi^{T}$ , with RMS 90% larger than that of the compositional contribution, dln $\Phi^{C}$ . Comparison with Figure 7d further shows that heat flux maps are dominated directly

by temperature anomalies, i.e., by the first term in the right-hand-side of equation (14). Including the effect of temperature on conductivity increases the amplitude of heat flux anomalies by ~12% but does not modify the heat flux pattern (Figure 8e). Taking into the effect of composition further increases the amplitude of heat flux anomalies by ~7% and slightly modifies the pattern (Figure 8f). In particular, iron and bridgmanite variations induce a substantial heat flux decrease within LLSVPs, with a local minimum up to 50% lower than the mean heat flux. Heat flux anomalies decrease in amplitude with increasing  $\Delta T_{ref}$  (dark red curve in Figure 9a), due to the fact that  $\Phi_{ref}$  increases with  $\Delta T_{ref}$ . Furthermore, increasing  $\Delta T_{ref}$  decreases dln $\Phi^T$  but leaves dln $\Phi^C$  unchanged; i.e., as  $\Delta T_{ref}$  increases, the relative influence of compositional anomalies on heat flux becomes more important (blue curve in Figure 9a). The amplitude of dln $\Phi$  only slightly depends on the iron partitioning, with RMS varying from 0.296 to 0.284 for  $K_D$  in the range of 0.1–0.7. For  $\Delta T_{ref} = 750$  K, high heat flux anomalies, up to 70% larger than the mean heat flux, appear in regions where temperature is lower than average.

Amplitude and pattern of CMB heat flux anomalies may partially control the dynamics of the core. Dynamo actions may be lost if CMB heat flux variations are too high [*Olson and Christensen*, 2002]. The level of heat flux heterogeneity and its influence on the core dynamics are usually quantified with the  $q^*$  parameter, defined as

$$q^* = \frac{(\Phi_{\text{max}} - \Phi_{\text{min}})}{2\Phi_{\text{ref}}},$$
(15)

which may also be written  $q^* = (dln\Phi_{max} - dln\Phi_{min})/2$ . Again,  $q^*$  strongly depends on the mean vertical temperature jump  $\Delta T_{ref}$  (Figure 9b), and very slightly on the iron partitioning,  $K_D$ . For  $K_D = 0.25$ , our calculations indicate that  $q^*$  is equal to  $\approx 0.63$  for  $\Delta T_{ref} = 750$  K and drops to  $\approx 0.47$  for  $\Delta T_{ref} = 1250$  K. Furthermore, it is interesting to note that  $q^*$  is mainly controlled by the thermal contribution to heat flux anomalies (red curve in Figure 9b) and more particularly by the direct effect of temperature anomalies (green curve in Figure 9b). For instance, at  $\Delta T_{ref} = 750$  K,  $q^*$  is equal to 0.54 if thermal conductivity is assumed constant, 0.61 if changes in conductivity due to changes in temperature are taken into account, and 0.63 if changes in conductivity induced by both thermal and compositional anomalies are included. The compositional contribution increases substantially  $q^*$  only for  $\Delta T_{ref}$  larger than 700 K.

The values of  $q^*$  predicted by our modeling are usually considered as high enough to significantly alter geodynamo. There is, however, no consensus on the level of heterogeneity needed to affect the geodynamo. Values of  $q^* > 1$  have been reported for successful dynamos [*Dietrich and Wicht*, 2013], in contradiction with earlier estimates [*Olson and Christensen*, 2002]. Heat flux pattern derived from classical tomography is dominated by  $Y_2^2$  spherical harmonic terms and recovers well the locations of high-latitude intense geomagnetic flux patches on the CMB [*Gubbins et al.*, 2007]. Refined patterns with equatorially concentrated heat flux allow explaining low-latitude intense geomagnetic flux patches [*Amit et al.*, 2015]. In our model, the compositional contribution to CMB heat flux is dominated by a  $Y_2^2$  pattern with local highs along the equator (Figure 8d). However, due to temperature distribution in [*Trampert et al.*, 2004], the total heat flux map substantially deviates from a  $Y_2^2$  pattern (Figure 8f). A potential consequence is the concentration of magnetic field lines in regions where CMB heat flux is high, which, in our maps, are located north of Japan and at the southern tip of South-America. Note that these regions of high heat flux are imposed by the pattern of temperature anomalies (Figure 7a) and already appear on the heat flux built with constant thermal conductivity (Figure 7d).

### 6. Conclusions

In this study, we have measured the lattice thermal conductivity of Fe-bearing and (Fe,Al)-bearing bridgmanites to pressures near the lowermost mantle. We found that the thermal conductivity of Fe-bearing bridgmanite initially increases monotonically with pressure but drops significantly around 45 GPa due to the pressure-induced lattice distortion on iron sites, making the thermal conductivity at the lowermost mantle conditions twice smaller than previously thought. Our experiments and modeling underline the strong effect of iron on the thermal conductivity of bridgmanite at lowermost mantle and its impact on CMB heat flux. A more detailed description of lower mantle thermal conductivity and CMB heat flux, however, requires additional experiments, including simultaneous high *P-T* measurements on the lattice and radiative thermal conductivity of the (Fe,Al)-bearing bridgmanite, ferropericlase, and post-perovskite. This would in turn provide a better description of the lower mantle dynamics and new constraints for geodynamo models and associated magnetic field patterns.

#### Appendix A

#### A1. Individual Fraction of Iron in Bridgmanite and Ferropericlase

The individual fraction of iron in bridgmanite and ferropericlase,  $x_{Fe}^{Bm}$  and  $x_{Fe}^{Fp}$ , may be calculated from the global fraction of iron,  $X_{Fe}$ , and the fraction of bridgmanite in the aggregate,  $X_{Bm}$ , and of the iron partitioning between bridgmanite and ferropericlase,  $K_D$  (equation (6)). Following equation (5),  $x_{Fe}^{Fp}$  may be expressed as

$$x_{Fe}^{Fp} = \frac{X_{Fe} - X_{Bm} x_{Fe}^{Bm}}{(1 - X_{Bm})}.$$
 (A1)

Replacing  $x_{Fe}^{Fp}$  in equation (6) with its expression in equation (A1) defines a second-order polynomial in  $x_{Fe}^{Bm}$ , whose positive solution is

$$x_{\rm Fe}^{\rm Bm} = \frac{1 + (X_{\rm Bm} + X_{\rm Fe})(K_D - 1) - \sqrt{\left[1 + (X_{\rm Bm} + X_{\rm Fe})(K_D - 1)\right]^2 - 4X_{\rm Bm}(K_D - 1)K_DX_{\rm Fe}}}{2X_{\rm Bm}(K_D - 1)}.$$
 (A2)

A similar procedure leads to

$$x_{\text{Fe}}^{\text{Fp}} = -\frac{1 + (X_{\text{Bm}} - X_{\text{Fe}})(K_D - 1) - \sqrt{\left[1 + (X_{\text{Bm}} - X_{\text{Fe}})(K_D - 1)\right]^2 + 4(1 - X_{\text{Bm}})(K_D - 1)X_{\text{Fe}}}{2(1 - X_{\text{Bm}})(K_D - 1)}.$$
 (A3)

# A2. Relative Anomalies in Thermal Conductivity Due to Changes in the Fractions of Iron and Bridgmanite

Relative variations in thermal conductivity of an aggregate of bridgmanite and ferropericlase ( $\Lambda_{VRH}$ ) due to variations in the global fraction in iron ( $X_{Fe}$ ) and in the fraction of bridgmanite ( $X_{Bm}$ ) are given by equations (8) and (9), assuming that the thermal conductivity of the aggregate is described by the Voigt-Reuss-Hill average of the thermal conductivities of bridgmanite ( $\Lambda_{Bm}$ ) and ferropericlase ( $\Lambda_{Fp}$ ). Equations (8) and (9) involve partial derivatives of  $\Lambda_{VRH}$  with respect to  $\Lambda_{Bm}$  and  $\Lambda_{Fp}$ , and partial derivatives of  $\Lambda_{Bm}$  and  $\Lambda_{Fp}$ , with respect to  $X_{Fe}$  and  $X_{Bm}$ . These partial derivatives are listed below in equations (A4) to (A9).

$$\frac{\partial \Lambda_{VRH}}{\partial \Lambda_{Bm}} = \frac{1}{2} X_{Bm} \left\{ 1 + \frac{\Lambda_{Fp}^2}{\left[ (1 - X_{Bm}) \Lambda_{Bm} + X_{Bm} \Lambda_{Fp} \right]^2} \right\}$$
(A4)

$$\frac{\partial \Lambda_{\text{VRH}}}{\partial \Lambda_{\text{Fp}}} = \frac{1}{2} (1 - X_{\text{Bm}}) \left\{ 1 + \frac{\Lambda_{\text{Bm}}^2}{\left[ (1 - X_{\text{Bm}})\Lambda_{\text{Bm}} + X_{\text{Bm}}\Lambda_{\text{Fp}} \right]^2} \right\}$$
(A5)

$$\frac{\partial \Lambda_{Bm}}{\partial X_{Bm}} = \frac{1}{2X_{Bm}} \left[ 1 - 2x_{Fe}^{Bm} - \frac{(1 - X_{Bm}) + K_D X_{Bm} - X_{Fe}(K_D + 1)}{\sqrt{\left[1 + (X_{Bm} + X_{Fe})(K_D - 1)\right]^2 - 4X_{Bm}(K_D - 1)K_D X_{Fe}}} \right] \frac{\partial \Lambda_{Bm}}{\partial x_{Fe}^{Bm}}$$
(A6)

$$\frac{\partial \Lambda_{\rm Fp}}{\partial X_{\rm Bm}} = -\frac{1}{2(1-X_{\rm Bm})} \left[ 1 - 2x_{\rm Fe}^{\rm Fp} - \frac{(1-X_{\rm Bm}) + K_D X_{\rm Bm} - X_{\rm Fe}(K_D+1)}{\sqrt{\left[1 + (X_{\rm Bm} - X_{\rm Fe})(K_D-1)\right]^2 + 4X_{\rm Fe}(1-X_{\rm Bm})(K_D-1)}} \right] \frac{\partial \Lambda_{\rm Fp}}{\partial x_{\rm Fe}^{\rm Fp}} \quad (A7)$$

$$\frac{\partial \Lambda_{Bm}}{\partial X_{Fe}} = \frac{1}{2X_{Bm}} \left[ 1 - \frac{(1 - X_{Bm}) - K_D X_{Bm} + X_{Fe} (K_D - 1)}{\sqrt{\left[1 + (X_{Bm} + X_{Fe})(K_D - 1)\right]^2 - 4X_{Bm} (K_D - 1)K_D X_{Fe}}} \right] \frac{\partial \Lambda_{Bm}}{\partial x_{Fe}^{Bm}}$$
(A8)

$$\frac{\partial \Lambda_{Fp}}{\partial X_{Fe}} = -\frac{1}{2(1 - X_{Bm})} \left[ 1 + \frac{(1 - X_{Bm}) - K_D X_{Bm} + X_{Fe}(K_D - 1)}{\sqrt{\left[1 + (X_{Bm} - X_{Fe})(K_D - 1)\right]^2 + 4X_{Fe}(1 - X_{Bm})(K_D - 1)}} \right] \frac{\partial \Lambda_{Fp}}{\partial X_{Fe}^{Fp}}$$
(A9)

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